

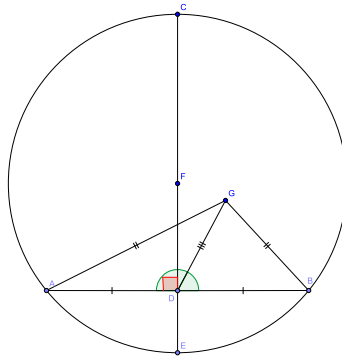
Proposition III.1

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Prop III.1: TO find the center of a given circle

-Let ABC be a circle

-Draw any straight line between two points on the circle, call it AB

-Bisect AB at D (I.10)

-Draw CE perpendicular to AB at D (I.11)

-Bisect CE at F (I.10)

-Claim: F is the center of the circle

-Suppose F is not the center, and let G be the center.

-Connect GA , GD , GB

- $AD = BD$, $GA = GB$ (both are radii), GD is common

-Thus, $\triangle GAD = \triangle GBD$ (I.8)

-Therefore, $\angle GDA = \angle GDB$

-Then, $\angle GDA = \angle GDB$ and both are right angles (Def I.10)

-But, $\angle FDB$ is a right angle, and $\angle GDB$ is contained in $\angle FDB$ so $\angle GDB$ but

be less than a right angle, which leads us to a contradiction

Thus, G is not the center, and F is the center.

QEF

Comments: Points A, B, C are not specified at beginning of proof, and become specified throughout course of the proof. Also, if G lies on CE , the proof still holds, as both would have to be radii of the circle, but one would be greater.

Porism: If in a circle, one straight line cuts another into two equal parts, and at right angles, then the center is on the cutting line.