

- (1) Verify the equivalence, up to mirroring, of the five knots described on the first day of class (you do not have to verify equivalence with the tangle toy model).
- (2) Determine the topological type of the surface depicted in the fourth description, using the classification of surfaces.
- (3) Starting from the fifth description, use the Seifert-van Kampen theorem to find a presentation for the fundamental group of the complement of the knot that has two generators and one relator.
- (4) Show that the complement of an unknotted curve in S^3 is diffeomorphic to an open solid torus and that the complement of the Hopf link is diffeomorphic to $T^2 \times (-1, 1)$.
- (5) Let D^2 denote the unit disk in \mathbb{R}^2 . Prove that if $f : D^2 \rightarrow \mathbb{R}^3$ is a smooth embedding, and $K = f(\partial D^2)$, then K is isotopic to $U = \{(x, y, 0) \in \mathbb{R}^3 \mid x^2 + y^2 = 1\}$. Hint: use the definition of $Df_{(0,0)}$ to define an isotopy from f to a linear map, adjust the resulting map by an affine transformation, and apply the isotopy extension theorem.